

Algebraic Representations of Dilations

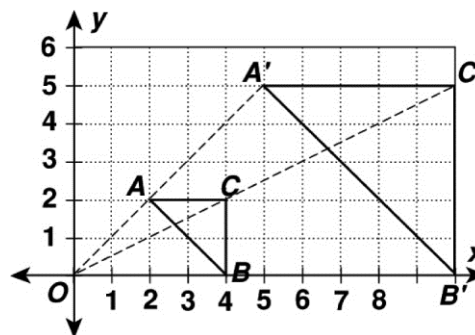
You dilate a figure using the origin as the center of dilation. Multiply each coordinate by the scale factor. The scale factor is the number that describes the change in size in a dilation.

Using the origin O as the center of dilation, dilate $\triangle ABC$ by a scale factor of 2.5.

$$A(2, 2) \rightarrow A'(2.5 \cdot 2, 2.5 \cdot 2) \text{ or } A'(5, 5)$$

$$B(4, 0) \rightarrow B'(2.5 \cdot 4, 2.5 \cdot 0) \text{ or } B'(10, 0)$$

$$C(4, 2) \rightarrow C'(2.5 \cdot 4, 2.5 \cdot 2) \text{ or } C'(10, 5)$$

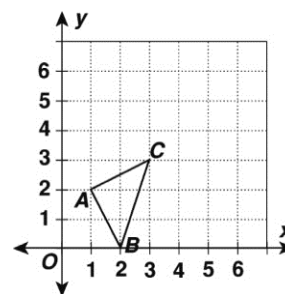


Using the origin as the center of dilation, dilate $\triangle ABC$ by a scale factor of 2. Graph the dilation.

$$1. A(1, 2) \rightarrow A'(2 \cdot 1, 2 \cdot 2) \text{ or } A'(\underline{\quad}, \underline{\quad})$$

$$B(2, 0) \rightarrow B'(\underline{\quad} \cdot 2, \underline{\quad} \cdot 0) \text{ or } B'(\underline{\quad}, \underline{\quad})$$

$$C(3, 3) \rightarrow C'(\underline{\quad} \cdot 3, \underline{\quad} \cdot 3) \text{ or } C'(\underline{\quad}, \underline{\quad})$$



When the scale factor is a fraction between 0 and 1, the image is smaller than the original figure.

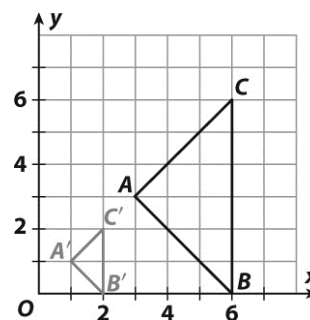
Using the origin O as the center of dilation, dilate

$\triangle ABC$ by a scale factor of $\frac{1}{3}$.

$$A(3, 3) \rightarrow A'\left(\frac{1}{3} \cdot 3, \frac{1}{3} \cdot 3\right) \text{ or } A'(1, 1)$$

$$B(6, 0) \rightarrow B'\left(\frac{1}{3} \cdot 6, \frac{1}{3} \cdot 0\right) \text{ or } B'(2, 0)$$

$$C(6, 6) \rightarrow C'\left(\frac{1}{3} \cdot 6, \frac{1}{3} \cdot 6\right) \text{ or } C'(2, 2)$$

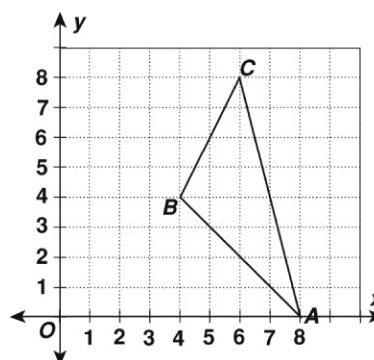


Using the origin as the center of dilation, dilate $\triangle ABC$ by a scale factor of $\frac{1}{2}$. Graph the dilation.

$$2. A(8, 0) \rightarrow A'\left(\frac{1}{2} \cdot 8, \frac{1}{2} \cdot 0\right) \text{ or } A'(\underline{\quad}, \underline{\quad})$$

$$B(4, 4) \rightarrow B'(\underline{\quad} \cdot 4, \underline{\quad} \cdot 4) \text{ or } B'(\underline{\quad}, \underline{\quad})$$

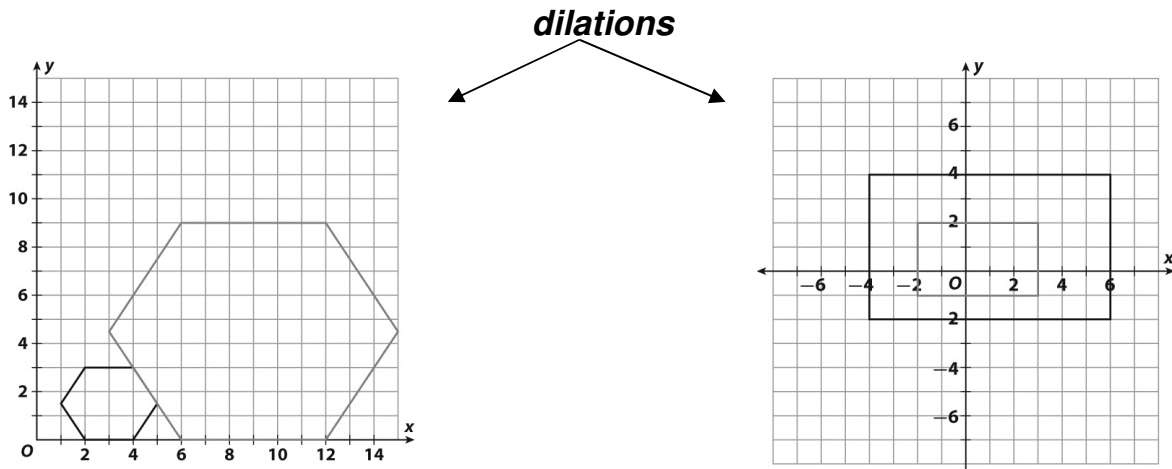
$$C(6, 8) \rightarrow C'(\underline{\quad} \cdot 6, \underline{\quad} \cdot 8) \text{ or } C'(\underline{\quad}, \underline{\quad})$$



Algebraic Representations of Dilations

Reading Strategies: Build Vocabulary

A **dilation** changes the size of a figure without changing its shape. Some dilations are **enlargements**. Some dilations are **reductions**.



The gray figure is an **enlargement**.

The gray figure is a **reduction**.

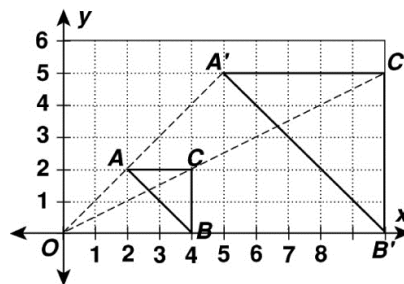
The gray figures are called **images** of the black figure.

The black figures are the original figures.

Sometimes the original figures are called **preimages**.

Vertices of original figures or preimages are indicated with italic capital letters. For example, ABC .

Vertices of dilated figures or images are indicated with italic capital letters followed by a small mark called a prime symbol. For example, $A'B'C'$.



Complete.

- The figures at the right show a reduction. Label the vertices of the original figure MNP . Label the vertices of the dilation $M'N'P'$.
- Explain the difference between an enlargement and a reduction.

